

# WAGES AND PRODUCTIVITY GROWTH IN A COMPETITIVE INDUSTRY\*

Helmut Bester

Department of Economics, Free University Berlin, Germany,

E-mail: hbester@wiwiss.fu-berlin.de

and

Emmanuel Petrakis

Department of Economics, University of Crete, Greece

E-mail: petrakis@econ.soc.uoc.gr

Final version January 2002,  
forthcoming in JOURNAL OF ECONOMIC THEORY

Running Title:

Productivity Growth

Mailing Address:

Prof. H. Bester

Dept. of Economics

Free University Berlin

Boltzmannstr. 20

D-14195 Berlin (Germany)

E-mail: hbester@wiwiss.fu-berlin.de

tel: +49 30 838 55257, fax: +49 30 838 54142

---

\*The first author is grateful for financial support from the German Science Foundation (DFG) under the programme “Industrieökonomik und Inputmärkte”.

## Abstract

We describe the evolution of productivity growth in a competitive industry with free entry and exit. The exogenous wage rate determines the firms' engagement in labor productivity enhancing process innovation. There is a unique steady state of the industry dynamics, which is globally asymptotically stable. In the steady state, the number of active firms, their unit labor cost and supply depend on the growth rate but not on the level of the wage rate. In addition to providing comparative statics of the steady state, the paper characterizes the industry's adjustment path. *Journal of Economic Literature* Classification Numbers: D24, D41, D92, J30

*Key words:* process innovation, industry dynamics, wages.

# 1 Introduction

How do wages affect the incentives for labor productivity enhancing innovation at the firm and the industry level? We address this question by studying the evolution of productivity growth in a competitive industry in which the last period's best technology is freely available to all competitors. Firms in this industry face an exogenous wage rate, which can be thought of as being determined in the aggregate labor market of the underlying economy. This wage affects the innovative performance of the industry as firms seek to capture inframarginal rents by increasing labor productivity. The dynamics of innovation converge to a unique steady state, in which unit labor costs are constant over time. In the steady state, the number of active firms, their supply and unit labor cost turn out not to depend on the level of wages; they only depend on their rate of growth. From any initial configuration the industry characteristics monotonically approach the steady state as time evolves. Along the adjustment path, high but declining productivity growth rates are associated with entry of new firms and a decline in the size of firms. Exit induces an increase in market concentration when productivity growth is relatively low but increasing over time.

Technological innovations as a means to reduce labor costs seem to have been at the heart of economic growth for many decades. The conventional macroeconomic view is that productivity growth drives wage growth. In a competitive equilibrium, the wage rate equals the marginal productivity of labor. Therefore, traditional growth theory has a causality running from productivity growth to wage growth. This view, however, presumes that productivity growth is exogenous and independent of labor market conditions. In contrast, in our analysis productivity growth is endogenously determined by innovation incentives at the firm and industry level. Firms respond to high and growing wages by productivity enhancing innovations to substitute against labor. Our model thus points to a microeconomic causality that runs in the opposite direction to the traditional macroeconomic view.<sup>1</sup> It shows how wage growth, which may reflect technological progress at the economy-wide level, stimulates productivity enhancing innovations at the industry level. Of course, the implication of our partial equilibrium analysis for macroeconomic modelling is that both, wage growth and productivity growth, are jointly endogenously determined (see Hellwig and Irmen [15]).

Our theoretical argument is in the same spirit as the empirical findings of Gordon [10] who argues that a substantial component of accelerations and

---

<sup>1</sup>A similar causality is emphasized in efficiency wage models, where higher wages raise productivity because of adverse selection or incentive effects, see e. g. Yellen [30].

decelerations of productivity growth in Europe, Japan and the U.S. can be attributed to the behavior of the ratio of wages to labor productivity (see also Gordon [11]). A number of microeconomic studies have established a positive relationship between wages and the introduction of new technologies. The time series results of Doms, Dunne and Troske [6] suggest that plants with high wage workforces are more likely to adopt new technologies. A possible explanation for this could be some complementarity between technology and skill: Wages are positively related to workforce skills and these skills allow new technologies to be adopted at lower costs. The alternative rationalization, which we model in this paper, is that higher wages will induce firms to substitute away from labor through new technologies. Chennells and Van Reenen [3] conclude from their analysis of British plant data that this substitution effect may indeed be an important factor. In a dynamic factor demand model, Mohnen *et. al.* [25] find that the long-run cross-price elasticity of  $R\&D$  with respect to the price of labor is fairly large. Also Flaig and Stadler [9] conclude from their estimation of a dynamic model of innovation behavior that the wage rate seems to be a major determinant for process innovations.

The partial equilibrium dynamics of a competitive industry have been studied first by Lucas and Prescott [24]. Since then, a number of models has been developed that focus on innovation under technological uncertainty in a competitive industry. These models investigate the stochastic evolution of firms and entry and exit over the product life cycle.<sup>2</sup> Our study focuses on the relation between wages and labor productivity. For simplicity, it disregards *ex ante* firm heterogeneity. Since the last period's best technology is freely available to all potential competitors, entry and exit never occur simultaneously along the adjustment path as the industry variables approach their steady state values. Also, the basic model in Sections 2 – 4 abstracts from stochastic factors that may affect innovation. This, however, is not restrictive since, as we show in Section 5, uncertainty does not qualitatively alter our results. An interesting feature of our model is that innovation does not rely on monopoly or oligopoly rents. It thus provides a counterexample to the Schumpeterian view that such rents are necessary to support  $R\&D$  investments. In our model, firms have strictly convex production technologies, which generate inframarginal rents. As in Petrakis and Roy [26], these rents induce profit maximizing entrepreneurs to spend resources on innovation.

Our model emphasizes the dynamic nature of the innovation process.

---

<sup>2</sup>See, e.g., Dixit [5], Hopenhayn [16], [17], [18], Jovanovic [19], Jovanovic and MacDonald [20], Klepper [21], Lach and Rob [22], Lambson [23], and Ericson and Pakes [7]. Ericson and Pakes [8] address this question in an imperfectly competitive industry.

Current innovations upgrade the technological knowledge that has been acquired through past innovations. They render old technologies obsolete and unprofitable. Innovators benefit from the past *R&D* efforts of their rivals. Also, they affect the incentives for future innovations. These features resemble several building blocks in some recent models of endogenous growth (e.g., Aghion and Howitt [1], Grossman and Helpman [13]). The endogenous growth literature typically treats all industries as symmetric; it does not capture the mechanism that induces different sectors to adjust to economy wide technological progress. Our model addresses this issue by offering a *partial equilibrium* perspective of the mechanisms underlying the endogenous growth literature. It focuses on the determinants of technical change in an industry that may be thought of as being imbedded in an economy in which overall technological progress induces wages to increase over time. In this way, our analysis may complement the aggregate models of the endogenous growth literature. It provides a feedback mechanism between aggregate factor productivity growth and innovation activities at the industry level. Indeed, as Hellwig and Irmen [15] have shown recently, our model can be used as a starting point for a general equilibrium model, which simultaneously determines the aggregate rate of technical change and the innovation behavior of individual firms.

Our model predicts that the impact of labor market conditions on productivity may be important for understanding the innovative performance of different industries and countries. Our analysis emphasizes the role of higher wages in creating substitution away from labor that boosts productivity in a small sector embedded in an economy where the aggregate market for labor is competitive and individual firms take wages at the industry level as exogenously given. In contrast, other studies have been concerned with the impact of unions on wages and innovation. Here the conventional wisdom follows Grout's [14] argument that the union will appropriate some share of the rents from technological improvements. This tends to reduce the firm's incentive to innovate.<sup>3</sup> Yet, our main insights do not necessarily rely on the competitive labor market paradigm. Our analysis shows that not the level of wages but their growth rate is important for long-run productivity growth. Therefore, the possible presence of industry wage differentials does not affect our results as long as the time path of the industry's wage follows the same trend as the competitive wage.

The remainder of the paper is organized as follows. Section 2 presents a

---

<sup>3</sup>A short outline of the rent-sharing argument together with an empirical analysis can be found in Van Reenen [29]. Ulph and Ulph [28] present a model with different conclusions.

stylized model of a competitive industry. Section 3 describes its short-run equilibrium. The main results are contained in Section 4, which studies the industry's long-run behavior. Section 5 briefly discusses the role of uncertainty in the innovation process. The final Section offers concluding remarks. The proofs of the formal results in Sections 3 and 4 are relegated to an Appendix.

## 2 The Model

The model depicts the evolution of a competitive industry with free entry and exit. The firms produce a homogeneous good and take the market clearing price as fixed. Similarly, they behave competitively in the labor market by considering the wage rate as exogenous. Time is discrete and at each date there is a sufficiently large number of potential producers who have access to the current technology. Producers become active at date  $t$  by investing in capacity and engaging in process innovation to increase labor productivity. At date  $t + 1$  they employ labor to produce output. Given the intertemporal path of wages, the evolution of the industry is determined by the active firms' innovation behavior because this generates the technology at the next date, which is available to all firms. In the basic model the innovation process is deterministic; the analysis is extended to stochastic innovation outcomes in Section 5.

Formally, the model is specified as follows. At date  $t$  a firm invests in production capacity  $x_t$  and at date  $t + 1$  it hires labor  $n_{t+1}$ . Depending on its labor productivity  $a_{t+1}$  in period  $t + 1$ , its output  $y_{t+1}$  is given by the Leontief production function

$$y_{t+1} = \min [x_t, a_{t+1} n_{t+1}]. \quad (1)$$

Obviously it is optimal to set  $n_{t+1} = x_t/a_{t+1}$  and so the firm's output is equal to  $x_t$ . At date  $t + 1$  the competitive wage rate is  $w_{t+1}$  and the firm sells its output at the price  $p_{t+1}$ . Therefore, its operating profit is

$$R(x_t, p_{t+1}, c_{t+1}) \equiv [p_{t+1} - c_{t+1}] x_t, \quad (2)$$

where  $c_{t+1} \equiv w_{t+1}/a_{t+1}$  denotes the firm's unit labor cost.

At date  $t$ , each potential producer observes the process innovations performed by the active firms. As Klepper [21], we assume that after one period he can costlessly incorporate these innovations into his own technology. Thus current *R&D* generates an intertemporal spillover effect on the starting point

of future innovative and productive activity. Still, an active firm has a one-period monopoly over the technological improvements generated by its *R&D* activity in period  $t$ . We focus on labor productivity enhancing process innovation and assume that each firm can increase current productivity by the factor  $(1 + q)$  by investing the amount  $K(q)$ . Thus, if  $a_t$  describes the most advanced technology developed at date  $t - 1$ , a firm's labor productivity at  $t + 1$  becomes

$$a_{t+1} = (1 + q_t)a_t$$

by investing at date  $t$  the amount  $K(q_t)$  in process innovation.

The exogenous wage rate  $w_t$  grows at the rate  $\gamma > 0$  so that  $w_{t+1} = (1 + \gamma)w_t$ , with  $w_0 > 0$ . One possible interpretation is that  $\gamma$  represents the average growth rate of labor productivity in the entire economy. Therefore, also wages grow at the rate  $\gamma$  in the equilibrium of the economy-wide labor market. Since the industry under consideration constitutes only a small part of the whole economy, its impact on the equilibrium wage rate can be taken to be negligible.<sup>4</sup> Given the growth of wages, after investing  $K(q_t)$  in innovation at date  $t$ , the firm's labor cost per unit of output at the next date is

$$c_{t+1} = \frac{1 + \gamma}{1 + q_t} c_t. \quad (3)$$

Finally, to install the capacity  $x$ , a firm has to invest the amount  $C(x) + f$ , i.e. there is a fixed cost  $f > 0$  and a variable capacity cost  $C(x)$ . Therefore, a firm that commits to the investment  $K(q_t) + C(x_t) + f$  in capacity and innovation, expects to have the profit

$$\Pi(q_t, x_t | p_{t+1}, c_t) \equiv \delta R \left( x_t, p_{t+1}, c_t \frac{1 + \gamma}{1 + q_t} \right) - K(q_t) - C(x_t) - f. \quad (4)$$

where  $\delta \in (0, 1]$  denotes the common discount factor.

We denote the total mass of active firms at date  $t$  by  $n_t$ . In each period, the industry faces the (inverse) demand function  $P(\cdot)$  so that  $P(\bar{x})$  is the market clearing price for the aggregate supply  $\bar{x}$ . The assumption that demand is stationary over time is not essential for our analysis. We discuss this issue below in Section 4.

We maintain the following assumptions on inverse demand  $P(\cdot)$ , innovation costs  $K(\cdot)$  and capacity costs  $C(\cdot)$ :

---

<sup>4</sup> As we indicated in the Introduction, the industry's wage rate  $w_t$  does not have to be *identical* to the competitive wage rate. If  $\omega_t$  represents the competitive wage rate, then our analysis remains valid as long as there is an  $\alpha > 0$  such that  $w_t = \alpha \omega_t$ .

ASSUMPTION 1:  $P(0) = \bar{p} > 0$ ,  $P' < 0$ ,  $P(\infty) = 0$  and

$$\delta \bar{p} > \min_{x \geq 0} \left[ \frac{C(x) + f}{x} \right]. \quad (5)$$

ASSUMPTION 2:  $K(0) = 0$ ,  $K'(0) = 0$ ,  $K'(q) > 0$ ,  $K''(q) > 0$  for all  $q > 0$ ,  $K(q) \rightarrow \infty$  as  $q \rightarrow \infty$  and

$$K''(q) \geq \frac{K'(q)^2}{2K(q)}. \quad (6)$$

ASSUMPTION 3:  $C(0) = 0$ ,  $C'(0) = 0$ ,  $C'(x) > 0$ ,  $C''(x) > 0$  for all  $x > 0$ ,  $C(x)/x \rightarrow \infty$  as  $x \rightarrow \infty$ , and

$$C''(x) \geq \frac{2[C'(x)x - C(x)]}{x^2} \quad (7)$$

Condition (5) in Assumption 1 guarantees that demand is sufficiently high so that some producers are active whenever the wage rate is small enough. Assumptions 2 and 3 ensure that the cost functions are sufficiently convex to avoid problems with nonconvexities, which typically arise in *R&D* models (see, e.g., Dasgupta and Stiglitz [4]). It is easy to see that Assumption 2 requires that the elasticity of the marginal innovation cost  $K'(q)$  is at least twice the elasticity of the cost  $K(q)$ . Similarly, the last part of Assumption 3 is identical to assuming that the elasticity of the difference between the marginal cost,  $C'(x)$ , and the average cost,  $C(x)/x$ , is at least one. Assumptions 2 and 3 are satisfied for instance for  $K(q) = \kappa q^\alpha$  and  $C(x) = \chi x^\beta$  as long as  $\alpha \geq 2$  and  $\beta \geq 2$ .

### 3 Static Equilibrium

First, we consider the industry equilibrium at a particular date  $t$ . At this date, the wage rate  $w_t$  together with the labor productivity  $a_t$  determine the current wage-productivity ratio  $c_t$ . This parameter describes the state of the industry at date  $t$ . Of course,  $c_t$  depends on the evolution of wages and productivity in the past. Yet, in this Section we focus on the static aspects of firm behavior and consider  $c_t$  as exogenous.

**Definition**  $(q_t^*, x_t^*, n_t^* | c_t)$  is a *static equilibrium* if

- (i)  $(q_t^*, x_t^*)$  maximizes  $\Pi(q, x | p_{t+1}, c_t)$  if  $n_t^* > 0$ ; and  $q_t^* = x_t^* = 0$  if  $n_t^* = 0$ ;



- (ii)  $\Pi(q_t^*, x_t^* | p_{t+1}, c_t) = 0$  if  $n_t^* > 0$ ; and  $\Pi(q, x | p_{t+1}, c_t) \leq 0$  for all  $(q, x)$  if  $n_t^* = 0$ ;
- (iii)  $p_{t+1} = P(n_t^* x_t^*)$ .

At date  $t$ , a total mass of  $n_t^*$  firms enters the market to produce some output at  $t + 1$ . Since all firms are identical, they choose the same output  $x_t^*$  and innovation rate  $q_t^*$ . The first equilibrium requirement is that the firms behave competitively by taking the market price  $p_{t+1}$  as fixed when choosing  $x_t^*$  and  $q_t^*$  so as to maximize profit. With free entry, profits cannot be positive. Condition (ii) states that each firm earns zero profit when the mass of active firms is positive. Otherwise, profits may be negative. Finally, as total output at date  $t + 1$  is  $n_t^* x_t^*$ , the third equilibrium condition ensures that the market clears at the price  $p_{t+1}$ .

**Proposition 1** *For each  $c_t$  there is a unique static equilibrium  $(q_t^*, x_t^*, n_t^* | c_t)$ . Moreover, there is a  $\bar{c} > 0$  such that  $n_t^* > 0$  if and only if  $c_t < \bar{c}$ .*

Proposition 1 establishes a unique static equilibrium for each wage–productivity ratio. If the wage rate is too high or the productivity of labor too low, then no firm enters the market because – even at the efficient scale – average costs exceed the chock-off price  $P(0)$ . If, however, the wage–productivity ratio is low enough, condition (5) ensures that a positive measure of firms operates in the market. Firms choose their  $R\&D$  expenditures such that their marginal benefit from the higher labor productivity tomorrow equals their marginal cost of innovation. Further, as firms are price takers, they choose the output level such that their marginal cost equals the market price. In addition, free entry in the industry implies that the firms’ average cost is equal to the market price, and hence to their marginal cost. As a consequence, it is as if each firm were minimizing its average costs in equilibrium. Given that a firm’s average cost is strictly convex in output and  $R\&D$  expenditures, there is a unique output and innovation level that minimizes these costs for each wage–productivity ratio; moreover, the minimum average cost, and thus the market price, is unique. Finally, the number of firms adjusts such that demand equals supply. As demand is strictly decreasing, the number of firms is uniquely determined in equilibrium.

**Proposition 2** *Let  $(q_t^*, x_t^*, n_t^* | c_t)$  be a static equilibrium. When  $c_t < \bar{c}$ , the rate of productivity growth  $q_t^*$  increases with the wage–productivity ratio  $c_t$ .*

Higher labor costs per unit of output create a stronger incentive to substitute away from labor through productivity enhancing innovation. This is simply so because firms choose their  $R\&D$  expenditures to equate the marginal benefit from the increase in labor productivity to the marginal cost of innovation. As the marginal benefit of innovation is proportional to the current wage-productivity ratio, the firm's optimal  $R\&D$  expenditures are higher when the current wage is higher, or the current labor productivity is lower.<sup>5</sup>

**Proposition 3** *Let  $(q_t^*, x_t^*, n_t^* | c_t)$  be a static equilibrium. When  $c_t < \bar{c}$ , each firm's output  $x_t$  increases with  $c_t$ . The total mass of active firms  $n_t^*$  and aggregate industry output  $n_t^* x_t^*$  strictly decrease with  $c_t$ .*

The rate of innovation and the level of output are complements for a profit maximizing firm. Intuitively, the total gain from a given reduction in unit labor costs increases with the quantity of goods produced. As we know already from Proposition 2, the higher the wage-productivity ratio, the higher is the firm's innovation rate. Accordingly, also output is positively related to the wage-productivity ratio. In other words, an increase in the unit labor cost raises the minimum efficiency scale, at which firms operate in a free entry equilibrium. Furthermore, since the minimum average cost is higher when a firm faces higher wages or its labor productivity is lower, the market clears at a higher price and total demand is reduced. Since bigger firms serve a smaller total demand, the number of active firms in the market is smaller when the wage-productivity ratio is higher.

Propositions 2 and 3 indicate that innovative investments are higher in a smaller, more concentrated market.<sup>6</sup> Yet, this observation does not imply a causal relationship since innovation, firm size and industry size are simultaneously determined. Another implication of Proposition 3 is that, as the wage-productivity ratio increases, aggregate employment in the industry decreases because industry output shrinks. As a result, higher productivity growth and lower aggregate employment are observed in the industry.<sup>7</sup> Note however that, as the size of firms increases, employment at the firm level may increase or decrease with the wage-productivity ratio. There is no clear relationship between productivity growth and employment at the plant level.

---

<sup>5</sup>See the first order conditions (16) in the Appendix.

<sup>6</sup>For our model, it would seem natural to regard  $1/n_t$  as a measure of the degree of concentration.

<sup>7</sup>This observation is in line with the model of Bean and Pissarides [2] where an upward shift in the wage-setting schedule raises both equilibrium unemployment and productivity growth.

## 4 Equilibrium Dynamics

We now turn to the industry dynamics which are determined by the firms' innovation decisions. At each date, free entry implies zero profits. Therefore, in period  $t$  each firm can ignore the impact of its innovation decision on the industry's state variable  $c_{t+1}$  at the subsequent date. In the previous Section it was shown how  $c_t$  affects the industry equilibrium in period  $t$ . As part of this equilibrium, the rate of productivity growth  $q_t^*$  is a function of  $c_t$ . Since  $q_t^*$  determines the change in the state variable from period  $t$  to  $t + 1$ , the industry's dynamics are generated by the evolution of  $c_t$ . The industry starts in period  $t = 0$  from the exogenously given labor productivity  $\bar{a}_0$ . Since the wage rate in this period is  $w_0$ , the initial value of the state variable is  $c_0 \equiv \bar{c}_0 = w_0/\bar{a}_0$ . We consider the parameter  $\bar{c}_0$  as exogenous and assume that it lies below the critical value  $\bar{c}$  specified in Proposition 1 so that  $n_0^* > 0$ .

**Definition**  $(q_t^*, x_t^*, n_t^* | c_t^*)_t$  is an *equilibrium sequence* if, for all  $t = 0, 1, \dots$ ,  $(q_t^*, x_t^*, n_t^* | c_t^*)$  is a static equilibrium and

$$c_{t+1}^* = \frac{1 + \gamma}{1 + q_t^*} c_t^*, \quad \text{with } c_0 = \bar{c}_0, \quad (8)$$

It follows immediately from Proposition 1 that for any  $\bar{c}_0$  the equilibrium path of the industry is fully determined. We are especially interested in the long-run behavior of the industry. Therefore, we look at the equilibrium outcome for large values of the time index  $t$  and investigate whether eventually the market will become stationary. The industry will be in a steady state if the number of active firms, their output and their innovation efforts remain constant over time.

**Definition**  $(\hat{q}, \hat{x}, \hat{n} | \hat{c})$  is a *steady state* if it is a static equilibrium and  $\hat{q} = \gamma$ .

In a steady state, the state variable remains at the value  $\hat{c}$  because wages and labor productivity grow at the same rate. As a result, also the number of active firms and their output do not change over time. Notice that, if there is a steady state, it is independent of the initial value  $\bar{c}_0$  of the state variable. Instead the steady state endogenously determines the wage-productivity ratio  $\hat{c}$ . Also, the definition of a steady state implicitly presumes that  $\hat{n} > 0$ . This follows immediately from the static equilibrium condition (i) and  $\gamma > 0$ .

**Proposition 4** *There is a  $\bar{\gamma} > 0$  such that a steady state  $(\hat{q}, \hat{x}, \hat{n} | \hat{c})$  exists if and only if  $\gamma < \bar{\gamma}$ . Moreover, if there is a steady state, it is unique.*

A steady state equilibrium is feasible only if the growth rate of wages is low enough so that the industry can afford to match it with labor saving innovations. If this is not the case, the evolution of productivity will lag behind the growth of wages and so average costs increase over time. Ultimately, this will drive the industry towards extinction as we show in Proposition 8 below. We will first deal with the more interesting case where  $\gamma < \bar{\gamma}$ . The following result shows that in this situation the time path of the industry will eventually approach the steady state, independently of the initial conditions.

**Proposition 5** *If there is a steady state, it is globally asymptotically stable. That is, as long as  $\gamma < \bar{\gamma}$ , the equilibrium sequence  $(q_t^*, x_t^*, n_t^* | c_t^*)_t$  converges to  $(\hat{q}, \hat{x}, \hat{n} | \hat{c})$  in the limit as  $t \rightarrow \infty$ .*

Over time, productivity growth converges to the rate of wage growth. Thus, the steady increase in real wages determines the firms' persistent engagement in labor productivity enhancing innovations. Another important implication of the above result is that the long-run behavior of the industry is independent of its initial productivity  $\bar{a}_0$  and the level of the wage rate  $w_0$ . As time evolves, the industry's innovative efforts adjust labor productivity in such a way that it becomes proportional to the wage rate by the factor  $1/\hat{c}$ . The basic intuition for this phenomenon is derived in Proposition 2. The incentives for innovation are positively related to the wage-productivity ratio. This ratio reaches its steady state level when productivity and wages grow at the same rate. Above this level it induces productivity to grow faster than wages. The opposite happens when unit costs are below the steady state value. As a result, the endogenous pace of technical progress always moves the wage-productivity ratio towards the steady state.

In the long-run, the initial state of the industry becomes irrelevant not only for  $c_t$  but also for  $q_t, x_t$  and  $n_t$ . These variables tend towards their steady state values, which are independent of  $\bar{a}_0$  and  $w_0$ . The level of wages, however, has a profound impact on the employment of labor. As  $\hat{c}$  is a constant, a one percent increase in the level of wages raises also the long-run level of labor productivity by one percent. At the same time, the level of wages does not affect total industry output in the steady state. As an implication, employment falls by one percent. In other words, the long-run elasticity of employment with respect to the wage level equals minus unity.

In the long-run, it is not the level of wages but the growth rate of wages which determines the industry's unit labor cost. As the following Proposition shows, the latter is positively related to the growth rate of wages.

**Proposition 6** *In the steady state  $(\hat{q}, \hat{x}, \hat{n}|\hat{c})$  the wage–productivity ratio  $\hat{c}$  increases with  $\gamma$ .*

Again, the intuition for this observation comes from Proposition 2. A higher rate of productivity growth can be supported only when higher unit labor costs force the firms to speed up innovation. In combination with Proposition 3, this implies that the steady state size of firms increases with  $\gamma$ . As a result of an increase in  $\gamma$ , a smaller number of firms operates in the industry producing a lower level of aggregate output.

We finally characterize the dynamic path of the industry.

**Proposition 7** *Let  $\gamma < \bar{\gamma}$ . Then the equilibrium sequence  $(q_t^*, x_t^*, n_t^*|c_t^*)_t$  satisfies*

$$q_t^* < q_{t+1}^* < \gamma, x_t^* < x_{t+1}^*, n_t^* > n_{t+1}^*, n_t^* x_t^* > n_{t+1}^* x_{t+1}^* \text{ if } \bar{c}_0 < \hat{c};$$

$$q_t^* > q_{t+1}^* > \gamma, x_t^* > x_{t+1}^*, n_t^* < n_{t+1}^*, n_t^* x_t^* < n_{t+1}^* x_{t+1}^* \text{ if } \bar{c}_0 > \hat{c}.$$

The industry monotonically approaches the steady state equilibrium. Depending on the initial state, the adjustment process exhibits either accelerations or decelerations of productivity growth. Changes in productivity growth are positively related with changes in firm size. Exit occurs in combination with relatively low but increasing rates of productivity growth. Along this path, the industry adjusts to a higher level of unit labor costs; total production and aggregate employment decrease while the output price increases. In contrast, when the industry approaches a lower level of unit labor costs, the industry’s production increases and so the output price declines over time. This process is supported by the entry of new firms, which exploit the knowledge-spillover externality created by the old firms.

The literature on industrial dynamics associates a ‘shakeout’ in the number of producers with the maturity phase in the industry’s product life cycle. As an empirical regularity of this phase (see, e.g., Gort and Klepper [12] and Klepper [21]), the number of producers steadily declines while their output increases. Also, the firms’ efforts to improve the production process increase over time. Proposition 7 reflects these regularities when  $\bar{c}_0 < \hat{c}$ . This parameter constellation might apply to an industry in which previous technological breakthroughs have lead to a high productivity level. Once the industry matures, the process of innovation becomes more predictable and is driven mainly by continuous technological improvements.

Given the initial state  $\bar{c}_0$ , exit occurs when wages grow relatively fast. Indeed, as we indicated above, the industry will not be able to reach a steady state when  $\gamma$  exceeds the critical level  $\bar{\gamma}$ . In this situation, the exit process eventually eliminates the entire industry.

**Proposition 8** *Let  $(q_t^*, x_t^*, n_t^* | c_t^*)_t$  be an equilibrium sequence. If  $\gamma > \bar{\gamma}$ , then there is a finite  $T > 0$  such that  $n_t^* = 0$  for all  $t \geq T$ .*

It is worth noting that in our model the demand function  $P(\cdot)$  has no effect on how  $q_t$ ,  $x_t$  and  $c_t$  are determined along the industry's equilibrium path. Indeed, profit maximization in combination with the assumption of free entry implies that, for a given  $c_t$ , each individual firm operates at the minimum of its average cost, which uniquely determines its choice of  $q_t$  and  $x_t$ . Therefore, these variables and the evolution of  $c_t$  are determined solely by the firms' cost structure and the growth rate of wages and are thus independent of demand.

Demand, however, does affect the number  $n_t$  of active firms. While the individual firm's technology is strictly convex, at the level of the industry constant returns are guaranteed by the assumption that the current technology can be replicated by those firms that decide to become active. In equilibrium, the price  $p_t$  equals the minimum of the individual firm's average cost and the number  $n_t$  of active firms adjusts to equate demand and supply. For example, an upward shift in the demand function  $P(\cdot)$  results in an increase of  $n_t$  along the equilibrium path but leaves all other variables unaffected.

As a consequence, stationarity of demand is not essential for our analysis. Implicitly, stationarity presumes that the growth of wages and income in the economy does not affect industry demand. This could be justified by assuming that demand is derived from quasi-linear utility functions. If, however, demand does change over time, our analysis can easily be modified to take this into account. For instance, when demand grows at the rate  $\rho$ , then in the steady state also the number of active firms grows at the rate  $\rho$ . But,  $\rho$  does not influence  $\hat{q}$ ,  $\hat{x}$  and  $\hat{c}$ . Employment either increases or decreases over time depending on  $\rho$  being larger or smaller than  $\gamma$ .

## 5 Uncertain Innovations

To simplify the exposition of our key argument, we have so far modeled productivity enhancing innovations as a completely deterministic process.

By spending  $K(q_t)$  in productivity enhancing innovations at date  $t$ , a firm increases its labor productivity from  $a_t$  at date  $t$  to  $a_{t+1} = a_t(1 + q_t)$  at date  $t + 1$ . However, as investment in innovation often entails stochastic elements, it may be worthwhile to examine the robustness of our analysis by considering uncertainty in the investment outcome. The simplest way to address this issue is to assume that if an individual firm invests  $K(q_t)$  at date  $t$ , with probability  $r$  its labor productivity increases to  $a_{t+1} = a_t(1 + q_t)$  at date  $t + 1$  and with probability  $1 - r$  remains the same so that  $a_{t+1} = a_t$ , where  $0 < r < 1$  is the firm-specific probability of success. As previously, each potential producer can costlessly incorporate the best available practice into his own technology at the next date. Observe that, since there is a continuum of firms in the industry, the probability that at least one of them succeeds in enhancing its labor productivity equals one. Therefore, all active and potential producers start out with the labor productivity  $a_t(1 + q_t)$  at date  $t + 1$ .

Interestingly, the introduction of uncertainty does not qualitatively alter our main findings. To see this, note that the present value of expected profits of an active firm is now

$$\begin{aligned} \Pi(q_t, x_t | p_{t+1}, c_t, r) &\equiv \delta \left[ p_{t+1} - r c_t \frac{1 + \gamma}{1 + q_t} - (1 - r) c_t (1 + \gamma) \right] x_t \quad (9) \\ &- K(q_t) - C(x_t) - f. \end{aligned}$$

In comparison with (4), uncertainty shifts the individual firm's (expected) average cost curve upwards and lowers the marginal benefit of the innovation effort.<sup>8</sup> Therefore, in the unique static competitive equilibrium with  $n_t^* > 0$  and a given  $c_t$ , the firm's innovation rate and output level are now lower, the expected average cost and thus the product price are higher, and the aggregate production level is lower. (Note that, the number of active firms, however, can be higher or lower.) Moreover,  $n_t^* > 0$  if and only if  $c_t < \bar{c}(r) < \bar{c}$ , with  $\partial \bar{c} / \partial r > 0$ , i.e. there is a positive number of active producers in the industry only for wage-productivity ratios that are lower than an upper-bound  $\bar{c}(r)$  which is smaller than under certainty and which decreases as the probability of success becomes smaller.

Turning to the equilibrium dynamics, there exists a unique steady state where the (industry) labor productivity growth rate equals again the exogenous growth rate in wages  $\gamma$  if and only if  $\gamma < \bar{\gamma}(r) < \bar{\gamma}$ , with  $\partial \bar{\gamma} / \partial r > 0$ . That is, the upper bound is lower under uncertainty and decreases as the

---

<sup>8</sup>Note that, a decrease in the probability of success  $r$  has the same impact on the marginal benefit of the investment as a decrease in the individual firm's discount factor  $\delta$ .

probability of success becomes smaller. Hence, the industry becomes extinct even for growth rates of wages where it could survive under deterministic innovations. Otherwise, the industry converges monotonically towards the steady state where the (industry) innovation rate equals  $\gamma$ . In the steady state, each active firm invests  $K(\gamma)$  in labor productivity enhancing processes at date  $t$  and obtains positive profits at date  $t + 1$  if it succeeds in innovating and negative profits in case of failure, with its expected profits at date  $t$  being equal to zero. Finally, the wage-productivity ratio in the steady state is higher than under certainty, i.e.  $\hat{c}(r) > \hat{c}$  and, moreover, increases as  $r$  becomes smaller, i.e.  $\partial \hat{c} / \partial r < 0$ . Intuitively, the firms will invest less for each given wage-productivity ratio, because their incentives to invest in labor saving innovations are weaker under uncertainty. As a result, the industry will now match the rate of wage growth only if the wage-productivity ratio is higher than with deterministic innovations.

## 6 Concluding Remarks

Technical progress and a substantial increase in real wages are main attributes of the growth process in the advanced industrial nations. Our analysis presents a cost-push argument of productivity growth. The basic idea is that profit seeking, competitive firms adjust their innovative activity to increasing labor costs. Higher labor costs create stronger incentives for process innovations that raise the productivity of labor. The more interesting issue, however, is the dynamic interaction between innovation and productivity. As current innovations aim at reducing the firms' labor cost, they also affect their future incentives for inventive activities. Our analysis shows that long-run productivity growth at the industry level is driven by the growth rate of wages. This rate determines the number of active firms, their labor costs per unit of output, the size of firms and the industry's output in the long-run. While these variables are independent of the level of the wage rate, the latter determines the level of labor productivity and employment within the industry. These results are derived in a basic model with a deterministic innovation process. Yet, it is shown that this model can easily be extended and that uncertainty does not qualitatively change the results.

The industry's adjustment path exhibits either entry or exit of firms. In contrast with a number of recent studies on industry dynamics, we abstract from stochastic factors that induce firm heterogeneity. Yet, this abstraction is mainly motivated by simplicity. In principle, our model could be enriched by firm-specific technological shocks so that entry and exit occur simultaneously.



Another interesting extension of our model is the consideration of imperfect competition. A Cournot or Bertrand framework could address the question of how strategic interactions between the firms affect productivity growth in the short-run and in the long-run. Stimulated by the work of Schumpeter [27], a large part of the literature on *R&D* relates the pace of innovative activity to market structure. An imperfect competition version of our model could combine this approach with our cost-push argument. Also, it would allow studying the impact of unionization on innovation. Rent sharing is likely to depress the short-run incentives for innovation. Yet, our results lead to the conjecture that unionization will not influence long-run productivity growth, unless wage bargaining affects not only the level but also the growth rate of industry wages.

## 7 Appendix

This Appendix contains the proofs of Propositions 1 – 8. These proofs are based on a series of lemmas that characterize the firms' average cost, which is given by

$$\varphi(q, x|c) \equiv \delta c \frac{1 + \gamma}{1 + q} + \frac{K(q) + C(x) + f}{x}. \quad (10)$$

**Lemma 1** *Let  $(q_t, x_t, n_t|c_t)$  be a static equilibrium. If  $n_t > 0$ , then  $(q_t, x_t)$  minimizes  $\varphi(q, x|c_t)$ . Moreover,  $\delta p_{t+1} = \varphi(q_t, x_t|c_t)$ .*

*Proof.* By equilibrium condition (ii),  $\delta p_{t+1} = \varphi(q_t, x_t|c_t)$ . Suppose there exists  $(q', x')$  such that  $\varphi(q', x'|c_t) < \varphi(q_t, x_t|c_t)$ . Then  $\Pi(q', x'|p_{t+1}, c_t) > 0 = \Pi(q_t, x_t|p_{t+1}, c_t)$ . This yields a contradiction to condition (i). Q.E.D.

**Lemma 2** *The function  $\varphi(q, x|c)$  is strictly convex in  $(q, x)$  for all  $(q, x) > 0$ .*

*Proof.* We have

$$\varphi_{qq} = \frac{2\delta c(1 + \gamma)}{(1 + q)^3} + \frac{K''(q)}{x} > 0, \quad \varphi_{qx} = -\frac{K'(q)}{x^2}, \quad (11)$$

and

$$\varphi_{xx} = \frac{2(K(q) + f)}{x^3} + \frac{C''(x)x^2 + 2C(x) - 2C'(x)x}{x^3} > 0. \quad (12)$$

This implies

$$\varphi_{xx}\varphi_{qq} - \varphi_{qx}^2 > \frac{K''(q)2K(q) - K'(q)^2}{x^4} \geq 0. \quad (13)$$

By the inequalities in (11) - (13),  $\varphi(q, x|c)$  is strictly convex. Q.E.D.

**Lemma 3** *Let  $(q(c), x(c))$  minimize  $\varphi(q, x|c)$ . Then  $q(\cdot)$  and  $x(\cdot)$  are continuous and strictly increasing in  $c$ . Moreover,  $q(c) \rightarrow 0$  as  $c \rightarrow 0$ ,  $q(c) \rightarrow \infty$  as  $c \rightarrow \infty$  and  $x(c) \rightarrow \infty$  as  $c \rightarrow \infty$ .*

*Proof.* By strict convexity of  $\varphi(\cdot)$  the values  $(q(c), x(c))$  are unique. The assumptions on  $K(\cdot)$  and  $C(\cdot)$  ensure that  $q(c) > 0$  and  $x(c) > 0$ . Since  $\varphi(\cdot)$  is continuous in  $(q, x, c)$  for all  $(q, x, c)$ , the functions  $q(\cdot)$  and  $x(\cdot)$  are continuous in  $c$ .

Let  $(q', x') = \operatorname{argmin} \varphi(q, x|c')$  and  $(q'', x'') = \operatorname{argmin} \varphi(q, x|c'')$ . Then

$$\begin{aligned} \delta c' \frac{1+\gamma}{1+q'} + \frac{K(q') + C(x') + f}{x'} &< \delta c' \frac{1+\gamma}{1+q''} + \frac{K(q'') + C(x'') + f}{x''}, \\ \delta c'' \frac{1+\gamma}{1+q''} + \frac{K(q'') + C(x'') + f}{x''} &< \delta c'' \frac{1+\gamma}{1+q'} + \frac{K(q') + C(x') + f}{x'}. \end{aligned} \quad (14)$$

Adding these inequalities yields

$$(c'' - c') \left( \frac{1+\gamma}{1+q''} - \frac{1+\gamma}{1+q'} \right) < 0. \quad (15)$$

Thus  $c' < c''$  implies that  $q'' > q'$ . This proves that  $q(\cdot)$  is strictly increasing. If  $\varphi(q, x|c)$  attains a minimum at  $(q, x)$ ,  $q$  and  $x$  must satisfy the first order conditions

$$\delta c(1+\gamma)x = K'(q)(1+q)^2, \quad C'(x)x - C(x) = K(q) + f. \quad (16)$$

The l.h.s. of the second equation is strictly increasing in  $x$  and the r.h.s. is strictly increasing in  $q$ . Therefore, as  $q(\cdot)$  is strictly increasing, also  $x(\cdot)$  is strictly increasing.

As  $x(\cdot)$  is strictly increasing, the first equation in (16) implies that  $q(c) \rightarrow 0$  as  $c \rightarrow 0$  and  $q(c) \rightarrow \infty$  as  $c \rightarrow \infty$ . The second equation in (16) therefore implies that also  $x(c) \rightarrow \infty$  as  $c \rightarrow \infty$ . Q.E.D.

**Lemma 4** *Let  $(q(c), x(c))$  minimize  $\varphi(q, x|c)$ . Then there is a unique  $\hat{c}$  such that  $q(\hat{c}) = \gamma$ . Moreover,  $q(c) < \gamma$  if  $c < \hat{c}$  and  $q(c) > \gamma$  if  $c > \hat{c}$ .*

*Proof.* By Lemma 3, one has  $q(c) < \gamma$  for  $c$  sufficiently small and  $q(c) > \gamma$  for  $c$  sufficiently large. Thus by continuity of  $q(\cdot)$  there is a  $\hat{c}$  such that  $q(\hat{c}) = \gamma$ . Uniqueness of  $\hat{c}$  and the second statement follow from Lemma 3, as  $q(\cdot)$  is strictly increasing. Q.E.D.

**Lemma 5** *Let  $(q(c), x(c))$  minimize  $\varphi(q, x|c)$ . Then  $c(1 + \gamma)/(1 + q(c))$  is increasing in  $c$ .*

*Proof.* Define  $z(c) \equiv c(1 + \gamma)/(1 + q(c))$ . Then rearranging the first equation in (16) yields

$$z(c) = \frac{K'(q(c))(1 + q(c))}{\delta x(c)}. \quad (17)$$

Thus we have  $z'(c) > 0$  if

$$[K''(q)(1 + q) + K'(q)]q'(c)x > x'(c)K'(q)(1 + q). \quad (18)$$

Differentiation of the second equation in (16) yields

$$C''(x)xx'(c) = K'(q)q'(c). \quad (19)$$

Therefore (18) is equivalent to

$$[K''(q)(1 + q) + K'(q)]C''(x)x^2 > [K'(q)]^2(1 + q). \quad (20)$$

By (7) this inequality is certainly satisfied if

$$\left[ \frac{K'(q)(1 + q)}{2K(q)} + 1 \right] [2C'(x)x - 2C(x)] > K'(q)(1 + q). \quad (21)$$

Since by (16)  $C'(x)x - C(x) = K(q) + f$ , this inequality is equivalent to

$$\left[ \frac{K'(q)(1 + q)}{2K(q)} + 1 \right] > \frac{K'(q)(1 + q)}{2[K(q) + f]}. \quad (22)$$

As  $f > 0$ , (22) is certainly satisfied, which proves that  $z'(c) > 0$ . Q.E.D.

*Proof of Proposition 1.* Let  $(q_t^*, x_t^*)$  be the argmin of  $\varphi(q_t, x_t|c_t)$  (see (10)). By Lemma 2,  $(q_t^*, x_t^*)$  is unique since  $\varphi$  is strictly convex in  $(q_t, x_t)$ . Define  $p_{t+1} \equiv \varphi(q_t^*, x_t^*|c_t)/\delta$ . Suppose first that  $p_{t+1} < P(0) = \bar{p}$ . Let  $n_t^*$  solve  $p_{t+1} = P(n_t^*x_t^*)$ . As  $P(\cdot)$  is strictly decreasing, the solution is unique with  $n_t^* > 0$ . We now claim that  $(q_t^*, x_t^*, n_t^*)$  is the unique static equilibrium for the wage-productivity ratio  $c_t$ . As  $(q_t^*, x_t^*)$  minimizes the average cost  $\varphi(\cdot|c_t)$ ,

it also maximizes a firm's profits for given  $p_{t+1}$  and thus condition (i) of the definition of the static equilibrium is satisfied. Further, by definition of  $p_{t+1}$  a firm makes zero profits (condition (ii)). Finally, by the definition of  $n_t^*$ , the market clears (condition (iii)). Suppose next that  $p_{t+1} \geq \bar{p}$ . In this case,  $n_t^* x_t^* > 0$  implies negative profits for all active firms. Hence, the unique static equilibrium is  $n_t^* = q_t^* = x_t^* = 0$ .

To prove the second part, note first that  $\varphi(q_t^*, x_t^* | c_t)$  is strictly increasing in  $c_t$  by the Envelope Theorem. Further,  $\varphi(q_t^*, x_t^* | c_t) > C(x_t^*)/x_t^*$ . Thus, by Lemma 3,  $\varphi(q_t^*, x_t^* | c_t) \rightarrow \infty$  as  $c_t \rightarrow \infty$ . Further, by (5),  $\varphi(q_t^*, x_t^* | 0) < \delta \bar{p}$ . Thus, by continuity of  $\varphi(\cdot)$ , there exists a  $\bar{c}$  such that  $\varphi(q_t^*, x_t^* | \bar{c}) = \delta \bar{p}$ . By the above argument,  $n_t^* > 0$  if and only if  $c_t < \bar{c}$ . Q.E.D.

*Proof of Proposition 2.* The statement follows immediately from Lemma 3. Q.E.D.

*Proof of Proposition 3.* The first statement follows immediately from Lemma 3. By Lemma 1,  $\delta P(n_t^* x_t^*) = \varphi(q_t^*, x_t^* | c_t)$ . Since by the Envelope Theorem,  $\varphi(q_t^*, x_t^* | c_t)$  is strictly increasing in  $c_t$ , this implies that  $n_t^* x_t^*$  decreases with  $c_t$ . As a consequence of the first statement, also  $n_t^*$  decreases with  $c_t$ . Q.E.D.

*Proof of Proposition 4.* Since  $\hat{n} > 0$ , Lemma 1 implies that  $\varphi(\gamma, \hat{x} | \hat{c}) \leq \varphi(q, x | \hat{c})$  for all  $(q, x)$ . By Lemma 4 there is a unique  $\hat{c}$  such that this condition is satisfied. By Proposition 1 there is thus a (unique) steady state if and only if  $\hat{c} < \bar{c}$ . It follows from Lemma 3 that  $q(\hat{c}) = \gamma$  and  $\hat{c} < \bar{c}$  if and only if  $\gamma$  lies below some positive upper bound  $\bar{\gamma}$ . Q.E.D.

*Proof of Proposition 5.* By Lemma 4,  $q_t^* < \gamma$  if  $c_t^* < \hat{c}$  and  $q_t^* > \gamma$  if  $c_t^* > \hat{c}$ . By (8) this implies

$$c_t^* < c_{t+1}^* \text{ if } c_t^* < \hat{c}; \quad c_t^* > c_{t+1}^* \text{ if } c_t^* > \hat{c}. \quad (23)$$

Lemma 5 in combination with (8) shows that  $c_{t+1}^*$  increases with  $c_t^*$ . This together with (23) yields

$$c_t^* < c_{t+1}^* < \hat{c} \text{ if } c_t^* < \hat{c}; \quad \hat{c} < c_{t+1}^* < c_t^* \text{ if } c_t^* > \hat{c}. \quad (24)$$

This proves that the sequence  $(c_t^*)_t$  converges. By (8), therefore,  $q_t^* \rightarrow \gamma$  so that  $c_t^* \rightarrow \hat{c}$ . By Proposition 1 and a simple continuity argument this implies that the equilibrium sequence converges to the steady state. Q.E.D.

*Proof of Proposition 6.* Let  $\gamma' < \gamma''$  and let  $(\gamma', x', n' | c')$  and  $(\gamma'', x'', n'' | c'')$  be the corresponding steady states. Suppose  $c' \geq c''$ . Then Proposition 2 implies that  $\gamma' \geq \gamma''$ , a contradiction. Q.E.D.

*Proof of Proposition 7.* By the proof of Proposition 5, the equilibrium sequence satisfies (24). This in combination with Propositions 2 and 3 proves the statement of the Proposition. Q.E.D.

*Proof of Proposition 8.* Suppose  $n_T^* > 0$  for all finite  $T$ . Then the proof of Proposition 5 implies that  $c_t^*$  converges to some  $\hat{c}$ . By Proposition 4,  $\hat{c} > \bar{c}$ . By Proposition 1 this implies  $n_t^* = 0$  for  $t$  sufficiently large, a contradiction. Since  $n_T^* = 0$  implies  $0 = q_t^* < \gamma$ , one has  $c_t^* > c_T^*$  for all  $t > T$ . Therefore  $n_t^* = 0$  for all  $t > T$ . Q.E.D.

## References

- [1] P. Aghion and P. Howitt, A Model of Growth through Creative Destruction, *Econometrica* **60** (1992), 323-51.
- [2] C.R. Bean and C. A. Pissarides, Unemployment, Consumption and Growth, *Europ. Econ. Rev.* **37** (1993), 837-854.
- [3] L. Chennells and J. Van Reenen, Technical Change and Earnings in British Establishments, *Economica* **64** (1997), 587-604.
- [4] P. Dasgupta and J. Stiglitz, Industrial Structure and the Nature of Innovative Activity, *Econ. J.* **90** (1980), 266-293.
- [5] A. Dixit, Entry and Exit Decisions under Uncertainty, *J. Polit. Economy* **97** (1989), 620 - 638.
- [6] M. Doms, T. Dunne, and K. R. Troske, Workers, Wages and Technology, *Quart. J. Econ.* **112** (1997), 253-290.
- [7] R. Ericson and A. Pakes, Empirical Implications of Alternative Models of Firm Dynamics, Working Paper, Yale University, 1990.
- [8] R. Ericson and A. Pakes, Markov-Perfect Industry Dynamics: A Framework for Empirical Work, *Rev. Econ. Stud.* **62** (1995), 53-82.
- [9] G. Flaig and M. Stadler, Success Breeds Success: The Dynamics of the Innovation Process, *Empirical Econ.* **19** (1994), 55-68.
- [10] R. J. Gordon, Productivity, Wages, and Prices Inside and Outside of Manufacturing in the US, Japan, and Europe, *Europ. Econ. Rev.* **31** (1987), 685 - 733.
- [11] R. J. Gordon, Interpreting the ‘One Big Wage’ in US Long-Term Productivity Growth, CEPR Discussion Paper No. 2608, 2000.
- [12] M. Gort, and S. Klepper, Time Paths in the Diffusion of Product Innovations, *Econ. J.* **92** (1982), 630-653.
- [13] G. M. Grossman and E. Helpman, Quality Ladders in the Theory of Growth, *Rev. Econ. Stud.* **58** (1991), 43-61.
- [14] P. A. Grout, Investment and Wages in the Absence of Binding Contracts: A Nash Bargaining Approach, *Econometrica* **52** (1984), 499-460.

- [15] M. Hellwig and A. Irmen, Endogenous Technical Change in a Competitive Economy, *J. Econ. Theory*, **101** (2001), 1-39.
- [16] H. A. Hopenhayn, Entry, Exit, and Firm Dynamics in Long Run Equilibrium, *Econometrica* **60** (1992), 1127-50.
- [17] H. A. Hopenhayn, Exit, Selection and the Value of Firms, *J. Econ. Dynam. Control* **16** (1992), 621-53.
- [18] H. A. Hopenhayn, The Shakeout, Economics Working Paper # 33, University of Pompeu Fabra, Barcelona, 1993.
- [19] B. Jovanovic, Selection and the Evolution of Industry, *Econometrica* **50** (1982), 649-70.
- [20] B. Jovanovic, and G. H. MacDonald, The Life Cycle of a Competitive Industry, *J. Polit. Economy* **102** (1994), 322-347.
- [21] S. Klepper, Entry, Exit, Growth, and Innovation over the Product Life Cycle, *Amer. Econ. Rev.* **86** (1996), 562-583.
- [22] S. Lach and R. Rob, R&D, Investment, and Industry Dynamics, *J. Econ. Manage. Strategy* **5** (1996), 217-249.
- [23] V. E. Lambson, Industry Evolution with Sunk Costs and Uncertain Market Conditions, *Int. J. Ind. Organ.* **9** (1991), 171 - 196.
- [24] R. E. Lucas and E. C. Prescott, Investment under Uncertainty, *Econometrica* **39** (1971), 659-681.
- [25] P. A. Mohnen, M. I. Nadiri and I. R. Prucha, R&D, Production Structure and Rates of Return in the US, Japanese and German Manufacturing Sectors, *Europ. Econ. Rev.* **30** (1986), 749-771.
- [26] E. Petrakis and S. Roy, Cost Reducing Investment, Competition and Industry Dynamics, *Int. Econ. Rev.*, **40** (1999), 381-401.
- [27] J. Schumpeter, "Capitalism, Socialism and Democracy", Allen and Unwin, London, 1947.
- [28] A. M. Ulph and D. T. Ulph, Labor Markets and Innovation: Ex-Post Bargaining, *Europ. Econ. Rev.* **38** (1994), 195-210.
- [29] J. Van Reenen, The Creation and Capture of Rents: Wages and Innovation in a Panel of U. K. Companies, *Quart. J. Econ.* **111** (1996), 195-226.

- [30] J. L. Yellen, Efficiency Wage Models of Unemployment,” *Amer. Econ. Rev.* (Proceedings) **74** (1984), 200-205.